The SLEAC Method

SLEAC is a low-resource method for *classifying* and *estimating* the coverage of selective feeding programs. It was designed to complement the SQUEAC method and is intended for use in programs delivering CMAM services over many *service delivery units*. Examples of such programs include:

- National or regional programs delivering CMAM services through health districts
- District programs delivering CMAM services through primary healthcare centres

SLEAC surveys *classify* coverage at the level of the service delivery unit. This will vary with the scale of the program. For example:

- In the case of a national or regional program delivering CMAM services through health districts (or the equivalent local administrative unit), the service delivery unit is the heath district and coverage is classified for an entire health district using a single SLEAC survey.
- In the case of a district program delivering CMAM services through primary healthcare centres, the service delivery unit is the primary healthcare centre and coverage is classified for each clinic's catchment area using separate SLEAC surveys.

It is **not** usually sensible to treat units larger than a health district or units smaller than a clinic catchment area as service delivery units.

SLEAC can also be used to estimate coverage over wide areas. SLEAC has been used for regional and national coverage surveys. In these surveys coverage is usually *classified* and *mapped* at the district level and *estimated* at the regional and national levels.

SLEAC may be used in a number of ways:

- As a quick and simple way of investigating (classifying) coverage in service delivery units that returns limited information on barriers to service access and uptake.
- To identify service delivery units that are failing to achieve coverage targets. SQUEAC investigations undertaken in some or all of the failing service delivery units are then used to inform program reforms. SLEAC surveys are repeated (after a suitable interval) to confirm progress. This process is illustrated in **Figure 67**.
- To identify service delivery units that are successfully meeting coverage targets and service delivery units that are failing to meet coverage targets. SQUEAC investigations are then undertaken in one or more of the succeeding and one or more of the failing service delivery units so that factors influencing program success and failure can be identified and used to inform program reforms. SLEAC surveys are repeated (after a suitable interval) to confirm progress. This process is illustrated in **Figure 68**.
- To classify and map coverage over wide areas in district, regional, and national coverage surveys.
- To estimate coverage over wide-areas in district, regional, and national coverage surveys.

The design intention is that rapid and relatively cheap SLEAC surveys can be used to effectively target more intensive and more expensive SQUEAC investigations, which are then used to inform program reforms (Figure 67 and Figure 68). SLEAC surveys are then used to confirm progress.

Figure 67. Using SLEAC and SQUEAC in failing service delivery units



Figure 68. Using SLEAC and SQUEAC in *succeeding* and *failing* service delivery units



SQUEAC and SLEAC are designed to complement each other:

SLEAC	SQUEAC
SLEAC is a wide-area method that can be used to classify and map the coverage of CMAM service at district, national, or regional levels.	SQUEAC is a local method used to identify factors influencing program success and failure at the local (i.e., district or clinic) level.
SLEAC provides a coarse overview of program coverage (i.e., coverage class) with only limited information on barriers.	SQUEAC provides a detailed view of program coverage and detailed information on barriers.

SLEAC may appear similar to the CSAS method. The key differences between the two methods are:

- SLEAC *classifies* coverage (e.g., as meeting or failing to meet a standard) at small scales, whereas CSAS *estimates* coverage at small scales (i.e., it returns a coverage proportion with a confidence interval).
- SLEAC can be used to map coverage classifications at the level of service delivery unit, whereas CSAS is intended to be used to map coverage in greater detail and usually *within* a service delivery unit (**Figure 69**).
- SLEAC can estimate coverage over several service delivery units, whereas CSAS usually estimates coverage for and within a single service delivery unit.
- A SLEAC survey will usually be very much quicker and very much cheaper than a CSAS survey of the same area.

Figure 69. The level of mapping available from SLEAC and CSAS methods

SLEAC

Districts are classified as having low, moderate, or high coverage. Regional or national mapping of program coverage is possible.





Classifying Program Coverage

The SLEAC method *classifies* program coverage for a service delivery unit such as a health district.

A SLEAC survey does **not** provide an estimate of overall program coverage with a confidence interval or credible interval for a single service delivery unit. Instead, a SLEAC survey identifies the category of coverage (e.g., 'low coverage' or 'high coverage') that describes the coverage of the service delivery unit being assessed. The advantage of this approach is that relatively small sample sizes (e.g., n = 40) are required to make an accurate and reliable *classification*.

SLEAC can estimate coverage over several service delivery units. Coverage is still classified for individual service delivery units. Data from the individual service delivery units are combined and coverage for this wider area is estimated from this combined sample.

SLEAC Survey Sample Design

The sample design used in SLEAC surveys is the same as that used in SQUEAC likelihood surveys:

First stage sampling method. This is the sampling method that is used to select the villages to be sampled. CSAS assessments use the *centric systematic area sampling* or *quadrat* method to select villages to be sampled. A similar method could be used to select villages to be sampled for the SQUEAC likelihood survey. The number of quadrats drawn on the map may be much smaller than would be used for a CSAS assessment (this is the same as using larger quadrats). The villages to be sampled may be selected by their proximity to the centre of each quadrat as is done in a standard CSAS survey (Figure 58 and Figure 59). The number and size of quadrats should be selected so as to spread the sample of villages over the entire program area. Many small quadrats are better than few large quadrats. For example, the sample illustrated in Figure 59 (19 quadrats) spreads the sample more evenly and over more of the program catchment area than the sample illustrated in Figure 58 (8 quadrats). You should use as many quadrats as is feasible with the time and resources available for the survey. The CSAS/quadrat sampling method is appropriate for estimating coverage over a wide area such as a health district. Another useful approach is to *stratify* by clinic catchment area and select villages systematically from a complete list of villages sorted by clinic catchment area (Figure 60). This approach may be used with any areas (e.g., administrative areas) for which complete lists of villages are available. The first stage sampling method should be a spatial sampling method that yields a reasonably even spatial sample from the entire program catchment area. Cluster sampling using PPS, such as that used for SMART surveys, is **not** appropriate. The stratified approach outlined above and illustrated in Figure 60 provides a reasonably even spatial sample using village lists and does not require the use of maps. It is important to note that sampling should **not** stop when the survey has reached its required sample size. Sampling stops only after you have sampled all of the the selected villages.

A within-community sampling method. This will usually be an active and adaptive casefinding method or a house-to-house *census* sampling method (see Box 3, page 65). These methods find all, or nearly all, current and recovering SAM cases in a sampled village. Sampling should be exhaustive. This means that you stop sampling only when you are sure that you have found all cases in the community. Sampling should **not** stop when you have met a quota or when the wider survey has reached its required sample size.

This is a two-stage sample because a sample of villages in the survey area is taken first (Stage 1) and then a 'census' sample of current and recovering SAM cases is taken from each and every one of the selected villages (Stage 2).

The CSAS/quadrat approach is useful for a single survey. If you repeat the survey then the same villages will be sampled. This may cause the survey to overestimate coverage because we expect coverage to have been improved by case-finding and referral in the sampled villages. One way around this problem is to sample villages at random from each quadrat. This will yield independent samples at each survey round. Do **not** exclude previously sampled villages. This may cause the survey to underestimate coverage and you will eventually run out of villages to sample.

SLEAC Survey Sample Size

SLEAC uses a *target sample size* (*n*) which, together with prevalence and population estimates, is used to decide the number of villages ($n_{villages}$) that should be sampled to achieve the target sample size.

A target sample size of 40 (n = 40) cases from each service delivery unit in which coverage is to be classified is usually large enough for most SLEAC applications.

In some settings, it may be difficult or even impossible to find 40 (n = 40) cases. This will be the case if service delivery units are small and/or the prevalence of SAM is low. In these situations, it is possible to use a smaller target sample size without increasing error. **Table 5** shows target sample sizes that may be used when the total number of cases in a service delivery unit is likely to be small. If, for example, the total number of cases in a service delivery unit is estimated to be about 60 cases then a target sample size of 25 cases may be used.

	Target sample size for				
Total number of cases in the service delivery unit [*]	50% standard	70% standard or 30%/70% class thresholds			
500	37	33			
250	35	32			
125	31	29			
100	29	26			
80	27	26			
60	25	25			
50	23	22			
40	21	19			
30	17	18			
20	15	15			

 Table 5. Target sample sizes for 50% and 70% coverage standards for use when surveying small service delivery units and/or the prevalence of SAM is low

* This is an estimate of the number of SAM cases in a service delivery unit at the time of the survey:

 $\left[\begin{array}{c} \textit{Population}_{\textit{all ages}} \times \frac{\textit{percentage of population}_{6-59\textit{months}}}{100} \times \frac{\textit{SAM prevalence}}{100} \right] \right]$

The target sample size (n), together with estimates of the prevalence of SAM in the survey area and population data, is used to calculate the number of villages $(n_{villages})$ that will need to be sampled to achieve the target sample size:

$$n_{\text{villages}} = \left[\frac{n}{\text{average village population}_{all ages} \times \frac{\text{percentage of population}_{6-59 \text{ months}}}{100} \times \frac{\text{SAM prevalence}}{100}\right]$$

SAM prevalence refers to the average SAM prevalence in the catchment area of the service delivery unit. It is unlikely that SAM prevalence will be known or known with good precision. SAM prevalence estimates may be available from previous nutritional anthropometry surveys (e.g., SMART surveys). SAM prevalence varies throughout the year (e.g., prevalence is usually higher before harvests than after harvests). This means that you should use the results from a nutritional anthropometry survey undertaken at the same time of year as the current SLEAC assessment. It is better to use a low rather than a high estimate of SAM prevalence for this sample size calculation. A value midway between the point estimate and the lower 95% confidence limit for SAM prevalence could be used. For example, if the prevalence of SAM is estimated as 1.2% (95% CI = 0.6% - 2.6%) then a suitable low estimate would be:

$$Prevalence = 1.2 - \frac{1.2 - 0.6}{2} = 0.9\%$$

Using a low estimate helps ensure that the survey will achieve the target sample size.

Note that prevalence here is the estimated prevalence of the program's admitting case definition. This will usually **not** be the weight-for-height based 'headline' prevalence estimate reported by a SMART survey. The required estimate will usually be found in the needs assessment section of a SMART survey report.

If you do not have nutritional anthropometry survey results from the same time of year as the current SQUEAC assessment then you should use results from the most recent nutritional anthropometry survey and adjust them using, for example, seasonal calendars of human disease (Figure 6, Figure 11, and Figure 12), calendars of food availability (Figure 6, Figure 11, and Figure 12), agricultural calendars (Figure 6, Figure 11, and Figure 19), long-term admissions data from nutrition programs (Figure 8), and long-term returns from growth monitoring programs.

The formula for the calculation of the minimum number of villages that need to be sampled to achieve the required sample size shown above assumes that the case-finding method being used will find all, or nearly all, current and recovering SAM cases in sampled villages. If you are not sure of this then you should sample a larger number of villages. You should monitor the number of cases that are found during the survey and be prepared to increase the number of villages that will be sampled if many fewer cases than expected are being found.

Once these decisions and calculations have been made, sampling locations can be identified and the survey undertaken. A standard questionnaire, such as that shown in Box 2 (page 49), should be applied to carers of non-covered cases found by the survey. Data collected using the standard questionnaire (Box 2) can be presented using a Pareto chart (a bar chart in which the bars are ordered by frequency) similar to those shown in Figure 2, Figure 45, and Figure 46).

Here is an example of the calculations required to decide the number of villages $(n_{villages})$ to sample:

Target sample size. A target sample size of n = 40 cases was selected. This is the standard sample size for a SLEAC survey.

Number of villages to be sampled. The following information was used to calculate the number of villages ($n_{villages}$) to be sampled:

Target sample size :	40
Average village population (all ages) :	475
Prevalence of SAM :	1.5%
Percentage of children aged between 6 and 59 months :	18%

The percentage of children aged between 6 and 59 months is usually assumed to be about 20% in developing countries. You should use 20% unless you have better information from, for example, a recent census or population survey.

Using this information, the number of villages to be sampled was calculated to be:

$$n_{\text{villages}} = \left[\frac{40}{475 \times \frac{18}{100} \times \frac{1.5}{100}}\right] = 32$$

When area sampling (see Figure 58 and Figure 59) is used, then the villages to be sampled are distributed evenly between the areas. For example, if a CSAS/quadrat sample with eight quadrats such as that shown in Figure 58 is used and 32 villages are to be sampled then:

$$\left[\frac{32}{8}\right] = 4$$

villages will need to be sampled from each quadrat.

In the case of a CSAS sample (e.g., Figure 58 and Figure 59), villages to be sampled are selected by their proximity to the centre of each quadrat (Figure 61). This selects clusters of villages and reduces the travel time between villages selected to be sampled. This allows more villages to be sampled by a survey team in a day.

A CSAS sample requires a map. If a map is not available then an alternative spatial stratification method may be used. Figure 60 shows a sample stratified by clinic catchment area. Any areal unit or subdivision for which complete lists of villages are available (e.g., counties, vice-counties, chiefdoms, electoral divisions) may be used. Figure 62, for example, illustrates the process of taking a spatially stratified systematic sample from a list of villages sorted by chiefdom. This type of sample also spreads the sample over the entire survey area.

Box 2 (page 49) shows an example of a simple structured interview questionnaire that may be applied to carers of non-covered cases found during the survey. The questionnaire shown in Box 2 yields qualitative data (i.e., questions regarding the *how?* and *why?* of decision making in carers of non-covered cases) that can be analysed using simple quantitative techniques as in Figure 2, Figure 45, and Figure 46).

Classifying Coverage in Individual Service Delivery Units

SLEAC uses the same simplified LQAS classification technique that is used in SQUEAC small-area surveys. The differences between how the simplified LQAS classification technique is used in SQUEAC and SLEAC are:

- The SLEAC survey sample is designed to represent the entire program area.
- A target sample size for SLEAC surveys is decided in advance of data collection.
- SLEAC surveys may classify coverage into three or more classes.

Analysis of data using the simplified LQAS classification technique involves examining the number of cases found in the survey sample (n) and the number of covered cases found:

- If the number of covered cases found exceeds a threshold value (*d*) then coverage is classified as being satisfactory.
- If the number of covered cases found does **not** exceed this threshold value (*d*) then coverage is classified as being unsatisfactory.

The threshold value (*d*) depends on the number of cases found (*n*) and the standard (*p*) against which coverage is being evaluated. A specific combination of *n* and *d* is called a *sampling plan*.

The following *rule-of-thumb* formula may be used to calculate a suitable threshold value (d) for any coverage proportion (p) and any sample size (n):

$$d = \left\lfloor n \times \frac{p}{100} \right\rfloor$$

For example, with a sample size of n = 40 and a coverage proportion (*p*) of 70% an appropriate value for *d* would be:

$$d = \left\lfloor n \times \frac{p}{100} \right\rfloor = \left\lfloor 40 \times \frac{70}{100} \right\rfloor = \left\lfloor 40 \times 0.7 \right\rfloor = 28$$

It is unlikely that a SLEAC survey will return the target sample size (n) exactly. If a survey does not return the target sample size (n) exactly then the classification threshold value (d) should be recalculated using the achieved sample size. For example:

Target sample size : 40
Achieved sample size : 43
Standard : 70%
$$d: \left[43 \times \frac{70}{100} \right] = 30$$

Coverage is classified using the same technique as is used for SQUEAC small-area surveys. For example:

Extending the Classification Method to Yield Finer Classifications

The simplified LQAS classification technique provides binary or two-tier classifications.

The method may be extended to provide more granular classifications.

Three classes are sufficient for most SLEAC applications. A three-tier classification method is particularly useful for identifying very high coverage service delivery units and very low coverage service delivery units for inclusion in subsequent SQUEAC investigations when using the SLEAC/SQUEAC strategy illustrated in Figure 68.

Three-tier classifications require two sampling plans/decision rules. These are created using the *rule-of-thumb* formula presented earlier.

For three-tier classifications there are two coverage proportions:

- p_1 : The upper limit of the 'low coverage' tier or class
- p_2 : The lower limit of the 'high coverage' tier or class

The 'moderate coverage' class runs from p_1 to p_2 . For example:



Two classification thresholds (d_1 and d_2) are used and are calculated as:



Classifications are made using the algorithm illustrated in Figure 70.

Figure 70. Algorithm for a three-class simplified LQAS classifier



This three-tier classification works well with small sample sizes (e.g., n = 40) provided that the difference between p_1 and p_2 is greater than or equal to about 20 percentage points.

Here is an example of the calculations required:

Sample size (n): 40

$$p_1$$
: 30%
 p_2 : 70%
 d_1 : $\left[n \times \frac{p_1}{100} \right] = \left[40 \times \frac{30}{100} \right] = 12$
 d_2 : $\left[n \times \frac{p_2}{100} \right] = \left[40 \times \frac{70}{100} \right] = 28$

Classifications are made using the algorithm illustrated in Figure 70. For example, using the calculations:

Sample size (n): 40

$$p_1$$
: 30%
 p_2 : 70%
 d_1 : $\left\lfloor n \times \frac{p_1}{100} \right\rfloor = \left\lfloor 40 \times \frac{30}{100} \right\rfloor = 12$
 d_2 : $\left\lfloor n \times \frac{p_2}{100} \right\rfloor = \left\lfloor 40 \times \frac{70}{100} \right\rfloor = 28$

the following classifications are made:

Number of covered cases	Classification
1, 2,, 12	LOW (i.e., < 30%) coverage
13, 14,, 28	MODERATE (i.e., between 30% and 70%) coverage
29, 30,, 40	HIGH (i.e., \geq 70%) coverage

Figure 71 shows a nomogram that can be used to find appropriate values for d_1 and d_2 given n, p_1 , and p_2 .



Figure 71. Simplified LQAS nomogram for finding appropriate values for d_1 and d_2 given n, p_1 , and p_2

If a survey does not return the target sample size (*n*) exactly then the classification thresholds (d_1 and d_2) should be calculated using the achieved sample size and classifications made using the algorithm illustrated in Figure 70. For example, a survey classifying coverage in individual clinic catchment areas using a target sample size of 40 (n = 40) cases for each catchment area and the class boundaries $p_1 = 30\%$ and $p_2 = 70\%$ returned the following data:

Clinic catchment area	Sample size	d_1^*	d_2^*	Number of covered cases	Classification
Chawama	38	11	26	29	High
Matero	32	9	22	18	Moderate
Makeni	43	12	30	36	High
Chipata	35	10	24	15	Moderate
Ngombe	42	12	29	14	Moderate
Kalingalinga	37	11	25	10	Low
Mtendere	39	11	27	5	Low
Kanyama	42	12	29	23	Moderate
All	308	92	215	150	Moderate

 d_1 and d_2 calculated after data collection using achieved sample sizes.

In this example, the target sample size was applied to each of the clinic catchment areas separately. This allows coverage classifications to be made for individual clinic catchment areas. This approach enables the identification of low coverage and high coverage service delivery units (clinics in this example) for subsequent SQUEAC investigations when using the SLEAC/SQUEAC strategies illustrated in Figure 67 and Figure 68. The example given here classifies coverage in clinic catchment areas in a single health district. These coverage classifications could be presented as a map:



A similar approach is applied to national or regional coverage surveys. In the case of national and regional coverage surveys, the service delivery units assessed by SLEAC should **not** be larger than individual health districts.

National and regional coverage surveys using SLEAC are stratified sample surveys in which strata are defined by health districts and sampled *exhaustively* (i.e., a SLEAC survey is undertaken in each and every health district in the nation). Such a survey will produce classifications of program coverage in each and every health district that can be mapped. Regional and national estimates of program coverage may also be produced (see below).

An alternative approach for identifying very high coverage service delivery units and very low coverage service delivery units for inclusion in subsequent SQUEAC investigations when using the SLEAC/SQUEAC strategies illustrated in Figure 67 and Figure 68 is to use coarse estimates of coverage:

 $Coverage = \frac{Number of covered cases}{Sample size}$

Clinic catchment area	Sample size	Number of covered cases	Coverage (%)	Selected for strategy in Figure
Chawama	38	29	$\frac{29}{38} \times 100 = 76\%$	Figure 68*
Matero	32	18	$\frac{18}{32} \times 100 = 56\%$	
Makeni	43	36	$\frac{36}{43} \times 100 = 84\%$	Figure 68
Chipata	35	15	$\frac{15}{35} \times 100 = 43\%$	
Ngombe	42	14	$\frac{14}{42} \times 100 = 33\%$	
Kalingalinga	37	10	$\frac{10}{37} \times 100 = 27\%$	Figure 67 [*] and Figure 68 [*]
Mtendere	39	5	$\frac{5}{39} \times 100 = 13\%$	Figure 67 and Figure 68
Kanyama	42	23	$\frac{23}{42} \times 100 = 55\%$	

in each surveyed area and pick the extreme values for further investigation:

* More than one 'best' and more than one 'worst' may be selected if there are a large number of areas and funding is available for additional SQUEAC investigations.

The advantage of using this approach is that there is no need to define high and low coverage categories in advance. This approach is also useful when the three-class method 'fails' and, for example, classifies all service delivery units as having low coverage.

Note that the coverage estimate is used solely for identifying the probable best and probable worst performing service delivery units.

Estimating Coverage over Wide Areas

It is also possible to *estimate* coverage over several service delivery units.

The number of SAM cases will vary between service delivery units in the program area. This means that the results from any one service delivery unit should be *weighted* by the number of cases in that service delivery unit.

The number of cases in each service delivery is unknown but can be estimated as:

$$N = \left[\begin{array}{c} \text{population of service delivery unit}_{allages} \times \frac{\text{percentage of population}_{6-59 \text{ months}}}{100} \times \frac{\text{SAM prevalence}}{100} \right]$$

The percentage of children aged between 6 and 59 months is usually assumed to be about 20% in developing countries. You should use 20% unless you have better information from, for example, a recent census or population survey.

If SAM prevalence is not known then a sensible guess should be used.

The weighting factor for each survey is:

$$w = \frac{N}{\sum N}$$

where:

N : Estimated number of cases in a surveyed service delivery unit

 $\sum N$: The sum of N over all surveyed service delivery units

The weighting factors for each survey (w) is based on estimates of the number of cases in each service delivery unit (N). These estimates are based on estimates of population size, population structure, and the prevalence of SAM:



The weighting factors should be as accurate as possible and be **local** to each survey. This means that, whenever possible, accurate and **local** estimates should be used to calculate the weighting factor (w).

Failure to use local estimates may cause too much or too little weight to be given to particular surveys. This may result in biased (i.e., inaccurate) wide area estimates of coverage. It may also make coverage appear to be patchy when it is, in fact, even (or vice versa).

Populations can change rapidly due to, for example, crisis displacement and population estimates from, for example, a past census may need to be adjusted.

The prevalence of SAM varies over both time and space. For example, neighbouring populations may have different prevalences of SAM due to differing food-economies, childcare practices, or patterns of disease. You should take care to use the appropriate **local** SAM prevalence estimate that is

available to you. It is almost never appropriate to use regional or national estimates of SAM prevalence from DHS or Multiple Indicator Cluster Survey (MICS) surveys.

Point coverage is estimated as:

$$Coverage = \sum \left[w \times \frac{c}{n} \right]$$

where:

w: weighting factor
$$W = \frac{N}{\sum N}$$
 for each survey (see above)

- c: number of covered cases found in each survey
- *n* : number of current cases attending the program plus the number of current cases **not** attending the program found in each survey

Period coverage may be estimated using the same formula with:

- c: number of current and recovering cases attending the program found in each survey
- *n* : number of current and recovering cases attending the program plus the number of current cases **not** attending the program found in each survey

The example data are for clinics within a single health district. The same method is used for national or regional coverage surveys that sample all districts in a nation (national coverage survey) or all districts within a region (regional coverage survey).

			P	opulation data	Survey data			Result	
Clinic	Pop.	6 – 59 months [*]	SAM prevalence*	Ν	$w = \frac{N}{\sum N}$	n	С	<u>c</u> n	$w \times \frac{c}{n}$
Chawama	28750	18.4%	2.2%	[28750×0.184×0.022]=115	115 900=0.13	38	29	$\frac{29}{38} = 0.76$	0.13×0.76=0.0988
Matero	22456	18.4%	2.2%	[22456×0.184×0.022]=90	90 900=0.10	32	18	$\frac{18}{32} = 0.56$	0.10×0.56=0.0560
Makeni	30050	18.4%	2.2%	[30050×0.184×0.022]=121	121 900=0.13	43	36	$\frac{36}{43} = 0.84$	0.13×0.84=0.1092
Chipata	28308	18.4%	2.2%	[28308×0.184×0.022]=114	114 900=0.13	35	15	$\frac{15}{35} = 0.43$	0.13×0.43=0.0559
Ngombe	24335	18.4%	2.2%	[24335×0.184×0.022]=98	98 900=0.11	42	14	$\frac{14}{42} = 0.33$	0.11×0.33=0.0363
Kalingalinga	25737	18.4%	2.2%	[25737×0.184×0.022]=104	104 900=0.12	37	10	$\frac{10}{37} = 0.27$	0.12×0.27=0.0324
Mtendere	32767	18.4%	2.2%	[32767×0.184×0.022]=132	$\frac{132}{900}$ =0.15	39	5	$\frac{5}{39} = 0.13$	0.15×0.13=0.0195
Kanyama	31 043	18.4%	2.2%	[31043×0.184×0.022]=125	$\frac{125}{900}$ =0.14	42	23	$\frac{23}{42} = 0.55$	0.14×0.55=0.0770
SUM		18.4%	2.2%	899	1.00	308	150		0.4851

Applying this method to the example clinic-level data gives:

* These data were available only at the district level and are the same for each clinic. If prevalence data for each clinic catchment area were available then *N* (the number of SAM cases) and *w* (the weighting factor) would have been calculated using the prevalence specific to each clinic catchment area.

The estimated coverage in the area served by the eight clinics is 0.4851 or 48.51%.

A 95% confidence interval on the estimated coverage can be calculated using the following formula:

95% CI = Coverage
$$\pm 1.96 \times \sqrt{\sum \frac{w^2 \times \frac{c}{n} \times \left(1 - \frac{c}{n}\right)}{n}}$$

Clinic	n	С	w	w ²	<u>c</u> n	$1-\frac{c}{n}$	$\frac{w^2 \times \frac{c}{n} \times \left(1 - \frac{c}{n}\right)}{n}$
Chawama	38	29	0.13	0.0169	$\frac{29}{38} = 0.76$	0.24	$\frac{0.0169 \times 0.76 \times 0.24}{38} = 0.00008112$
Matero	32	18	0.10	0.0100	$\frac{18}{32} = 0.56$	0.44	$\frac{0.0100 \times 0.56 \times 0.44}{32} = 0.00007700$
Makeni	43	36	0.13	0.0169	$\frac{36}{43} = 0.84$	0.16	$\frac{0.0169 \times 0.84 \times 0.16}{43} {=} 0.00005282$
Chipata	35	15	0.13	0.0169	$\frac{15}{35} = 0.43$	0.57	$\frac{0.0169 \times 0.43 \times 0.57}{35} \!=\! 0.00011835$
Ngombe	42	14	0.11	0.0121	$\frac{14}{42} = 0.33$	0.67	$\frac{0.0121 \times 0.33 \times 0.67}{42} \!=\! 0.00006370$
Kalingalinga	37	10	0.12	0.0144	$\frac{10}{37} = 0.27$	0.73	$\frac{0.0144 \times 0.27 \times 0.73}{37} = 0.00007671$
Mtendere	39	5	0.15	0.0225	$\frac{5}{39} = 0.13$	0.87	$\frac{0.0225 \times 0.13 \times 0.87}{39} = 0.00006525$
Kanyama	42	23	0.14	0.0196	$\frac{23}{42} = 0.55$	0.45	$\frac{0.0196 \times 0.55 \times 0.45}{42} = 0.00011550$
SUM	308	150					0.00065045

Applying this formula to the example data gives:

The 95% confidence interval is:

 $95\% CI = 0.4851 \pm 1.96 \times \sqrt{0.00065405} = \{43.51\%, 53.51\%\}$

It is usually only sensible to report an overall coverage estimate if:

- The overall sample size is about 96 (or larger). This sample size is usually sufficient for a 95% confidence interval of \pm 10 percentage points or better.
- Coverage is **not** patchy (i.e., coverage is broadly similar in each of the areas surveyed).

The patchiness of coverage can be assessed 'by eye' or using a *chi-square* test.

The chi-square test is a *statistical hypothesis test*. Statistical hypothesis tests such as the *chi-square test* rely on a *null hypothesis*. The *null hypothesis* states that nothing interesting is happening in the data other than random variation (e.g., coverage is **not** patchy). The *null hypothesis* is paired with an *alternative hypothesis* that states that something interesting or systematic is happening in the data (e.g., coverage **is** patchy).

Statistical hypothesis testing involves comparing what we would *expect* the data to look like if the *null hypothesis* were true with the collected or *observed* data. If the expected and observed data are very different from each other then we reject the *null hypotheses* and accept the *alternative hypothesis*.

If we are testing whether coverage is patchy then:

- The *null hypothesis* is that coverage is **not** patchy.
- The *alternative hypothesis* is that coverage **is** patchy.

The simplest illustration of using a *chi-square* test is to use it to compare the coverage of two service delivery units.

Consider the following data:

	Observed data				
Clinic	n	0			
Chawama	38	29			
Kalingalinga	37	10			

The *null hypothesis* is that coverage is **not** patchy. Another way of saying this is that coverage is *uniform* (i.e., the same) in both service delivery units. If the *null hypothesis* were true then we would expect the data to look like this:

	Observ	ed data	Expected data [*]
Clinic	n	0	E
Chawama	38	29	$\frac{39}{75} \times 38 = 19.76$
Kalingalinga	37	10	$\frac{39}{75} \times 37 = 19.24$
SUM	75 39		39

* These are the numbers we would expect to see if coverage in each clinic catchment area were the same as the average coverage across all clinic catchment areas.

These *expected values* (*E*) are the values we would expect to see if the *null hypothesis* were true.

The *expected values* are compared with the *observed values* (*O*) by subtracting them from the *observed values*:

	Observed data		Observed data Expected data		
Clinic	n	0	E	O-E	
Chawama	38	29	$\frac{39}{75} \times 38 = 19.76$	29-19.76=+9.24	
Kalingalinga	37	10	$\frac{39}{75} \times 37 = 19.24$	10-19.24=-9.24	
SUM	75	39	39	0	

The positive and negative differences cancel each other out. We square each difference to make them positive numbers:

	Observed data		Observed data Expected data		
Clinic	n	0	E	O-E	$(O-E)^2$
Chawama	38	29	$\frac{39}{75} \times 38 = 19.76$	29-19.76=+9.24	85.38
Kalingalinga	37	10	$\frac{39}{75} \times 37 = 19.24$	10-19.24=-9.24	85.38
SUM	75	39	39	0	

Before dividing them by the *expected values*:

	Observed data		Expected data			
Clinic	n	0	E	O-E	$(O - E)^2$	$\frac{(O-E)^2}{E}$
Chawama	38	29	$\frac{39}{75} \times 38 = 19.76$	29-19.76=+9.24	85.38	$\frac{85.38}{19.76}$ =4.32
Kalingalinga	37	10	$\frac{39}{75} \times 37 = 19.24$	10-19.24=-9.24	85.38	$\frac{85.38}{19.24}$ =4.44
SUM	75	39	39	0		8.76

The sum of these two numbers (8.76 in this example) is a measure of how much the *observed data* differ from the *expected values* under the *null hypotheses* and is called the *chi-square test statistic*.

Under the *null hypothesis* there is a fixed probability (called the *p-value* or just *p*) of obtaining a particular value for the *chi-square test statistic*:

- If the probability of obtaining a particular *chi-square test statistic* under the *null hypothesis* is large then the probability that the *null hypothesis* is true is also large. In this case, we would **accept** the *null hypothesis* (i.e., coverage is uniform) as being true.
- If the probability of obtaining a particular *chi-square test statistic* under the *null hypothesis* is small then the probability that the *null hypothesis* is true is also small. In this case, we would **reject** the *null hypothesis* and **accept** the *alternative hypothesis* (i.e., coverage is patchy) as being true.

It is common practice to define large as $p \ge 0.05$ and to define small as p < 0.05.

The value of the *chi-square test statistic* at p = 0.05 is known as the *critical value*. The value of the *chi-square test statistic* is compared to the *critical value*. If the *chi-square test statistic* is greater than the critical value then p < 0.05 and the *null hypothesis* is **rejected**.

The *critical value* of the *chi-square test statistic* changes with the number of surveys used to calculate the *chi-square test statistic* and is shown in **Table 6**.

There are two surveys in this example. The *critical value* of the *chi-square test statistic* for two surveys is 3.84 (see Table 6). Since 8.76 is greater than 3.84, we reject the *null hypothesis* and conclude that coverage is patchy.

Number of surveys	Critical value [*]	Number of surveys	Critical value*	Number of surveys	Critical value [*]
1	NA	13	21.03	25	36.42
2	3.84	14	22.36	30	42.56
3	5.99	15	23.68	40	54.57
4	7.81	16	25.00	50	66.34
5	9.49	17	26.30	60	77.93
6	11.07	18	27.59	70	89.39
7	12.59	19	28.87	80	100.75
8	14.07	20	30.14	90	112.02
9	15.51	21	31.41	100	123.23
10	16.92	22	32.67		
11	18.31	23	33.92		
12	19.68	24	35.17		

Table 6. Critical values of the chi-square test statistic

The *chi-square test statistic* can be used to assess patchiness over any number of service delivery units. The formula to calculate the chi-square test statistic is:

$$\chi^2 = \sum \frac{(O - E)^2}{E}$$

where:

- *O*: Number of covered cases *observed* in each surveyed service delivery unit.
- *E*: Number of covered cases *expected* in each surveyed service delivery unit if coverage is **not** patchy. You will need to calculate this.

The *chi-square* test presented here evaluates how much the observed numbers deviate from the numbers expected if coverage in each service delivery unit were the same as the overall coverage estimate.

If coverage is patchy then this should be noted in any report of the overall coverage estimate.

^{*} Corresponds to p = 0.05 on a chi-square statistic with N - 1 degrees of freedom

The table below applies the *chi-square* test to the example data:

Clinic catchment area	Sample size	0*	E**	$(0 - \mathbf{E})^2$	$\frac{\left(0-E\right)^2}{E}$
Chawama	38	29	$38 imes rac{150}{308} = 18.51$	$(29 - 18.51)^2 = 110.04$	$\frac{110.04}{18.51} = 5.94$
Matero	32	18	$32 imes rac{150}{308} = 15.58$	$(18 - 15.58)^2 = 5.86$	$\frac{5.86}{15.58} = 0.38$
Makeni	43	36	$43 imes rac{150}{308} = 20.94$	$(36 - 20.94)^2 = 226.80$	$\frac{226.80}{20.94} = 10.83$
Chipata	35	15	$35 \times \frac{150}{308} = 17.05$	$(15 - 17.05)^2 = 4.20$	$\frac{4.20}{17.05} = 0.25$
Ngombe	42	14	$42 \times \frac{150}{308} = 20.45$	$(14 - 20.45)^2 = 41.60$	$\frac{41.60}{20.45} = 2.03$
Kalingalinga	37	10	$37 \times \frac{150}{308} = 18.02$	$(10 - 18.02)^2 = 64.32$	$\frac{64.32}{18.02} = 3.57$
Mtendere	39	5	$39 imes rac{150}{308} = 18.99$	$(5 - 18.99)^2 = 195.72$	$\frac{195.72}{18.99} = 10.31$
Kanyama	42	23	$42 imes rac{150}{308} = 20.45$	$(23 - 20.45)^2 = 6.50$	$\frac{6.50}{20.45} = 0.32$
SUM	308	150***	150***		$\chi^{2} = 33.63$

* The number of covered cases *observed* in each survey

** The number of covered cases *expected* in each survey if coverage is **not** patchy

*** These columns should have the same total

The *chi-square test statistic* for the example data is 33.63.

The value of the chi-square test statistic is compared to a *critical value*. If the chi-square statistic is greater than the critical value then the coverage is patchy and it is more meaningful to report the disaggregated results than an overall coverage estimate. If you do report an overall coverage estimate then you should also report that the coverage was found to be patchy.

The critical value of the chi-square test statistic changes with the number of surveys used to calculate the chi-square test statistic and is shown in Table 6 (page 130). There are eight surveys in the example data. The critical value of the chi-square statistic for eight surveys is 14.07 (see Table 6). Since 33.63 is greater than 14.07, we conclude that coverage is patchy and it is better to report disaggregated results than an overall coverage or to report the overall coverage estimate **and** report that the coverage was found to be patchy.

Conclusions

SLEAC provides a quick and simple method for classifying coverage in program service delivery units and provides limited data (i.e., reasons for non-attendance collected from a single informant type using a single method with a small sample size) on barriers to service uptake and analysis. SLEAC offers program managers a method of targeting more intensive and expensive SQUEAC investigations when gathering evidence to inform program reforms. SLEAC also offers regional and national program managers a reasonably quick and simple method for mapping coverage over very wide areas.